

# Linear Programming

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**(2025)**

**Q.1** The corner points of the feasible region of a Linear Programming Problem are  $(0,2)$ ,  $(3,0)$ ,  $(6,0)$ ,  $(6,8)$  and  $(0,5)$ . If  $Z=ax+by$ ;  $(a, b>0)$  be the objective function, and maximum value of  $Z$  is obtained at  $(0, 2)$  and  $(3,0)$ , then the relation between  $a$  and  $b$  is : (1 Mark) (CBSE 2025 - 65/4/1)

A.  $a = 3b$

B.  $3a = 2b$

C.  $a = b$

D.  $b = 6a$

**Q.2 Assertion (A) :** In a Linear Programming Problem, if the feasible region is empty, then the Linear Programming Problem has no solution.

**Reason (R) :** A feasible region is defined as the region that satisfies all the constraints. (1 Mark) (CBSE 2025 - 65/4/1)

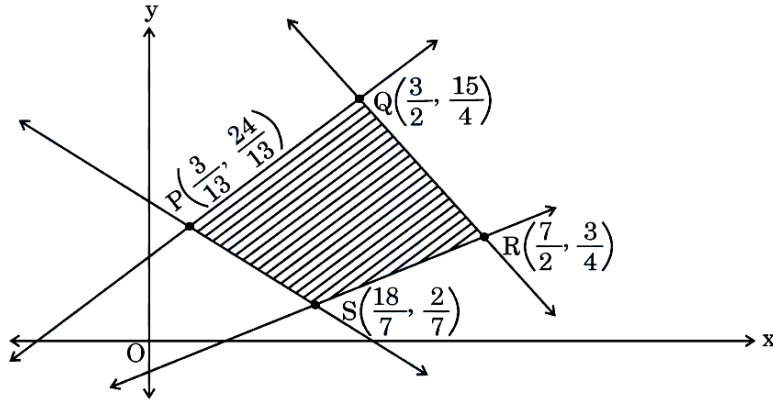
A. Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A).

B. Assertion (A) is true, but Reason (R) is false.

C. Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).

D. Assertion (A) is false, but Reason (R) is true.

**Q.3** For a Linear Programming Problem (LPP), the given objective function is  $Z=x+2y$ . The feasible region PQRS determined by the set of constraints is shown as a shaded region in the graph. (1 Mark) (CBSE 2025 - 65/6/1)



(Note : The figure is not to scale)

$$P \equiv \left(\frac{3}{13}, \frac{24}{13}\right), Q \equiv \left(\frac{3}{2}, \frac{15}{4}\right), R \equiv \left(\frac{7}{2}, \frac{3}{4}\right), S \equiv \left(\frac{18}{7}, \frac{2}{7}\right)$$

Which of the following statements is correct?

A. (Value of Z at P) > (Value of Z at Q)

B.

Z is maximum at R  $\left(\frac{7}{2}, \frac{3}{4}\right)$

C.

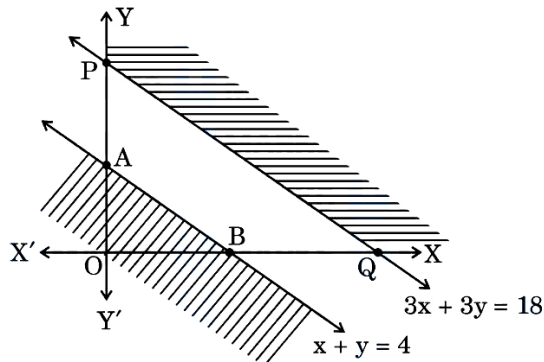
Z is minimum at S  $\left(\frac{18}{7}, \frac{2}{7}\right)$

D. (Value of Z at Q) < (Value of Z at R)

**Q.4** In a Linear Programming Problem (LPP), the objective function  $Z=2x+5y$  is to be maximised under the following constraints :

$$x+y \leq 4, 3x+3y \geq 18, x, y \geq 0$$

Study the graph and select the correct option. (1 Mark) (CBSE 2025 - 65/6/1)



(Note : The figure is not to scale)

**The solution of the given LPP :**

- A. lies in the combined region of  $\triangle AOB$  and unbounded shaded region.
- B. lies in the shaded unbounded region.
- C. does not exist.
- D. lies in  $\triangle AOB$ .

**Q.5 A factory produces two products X and Y . The profit earned by selling X and Y is represented by the objective function  $Z=5x+7y$ , where x and y are the number of units of X and Y respectively sold. Which of the following statement is correct? (1 Mark) (CBSE 2025 - 65/2/1)**

- A. The objective function measures the total production of products X and Y .
- B. The objective function maximizes the difference of the profit earned from products X and Y .
- C. The objective function maximizes the combined profit earned from selling X and Y.
- D. The objective function ensures the company produces more of product X than product Y

**Q.6 Assertion (A) :** Every point of the feasible region of a Linear Programming Problem is an optimal solution.

**Reason (R) :** The optimal solution for a Linear Programming Problem exists only at one or more corner point(s) of the feasible region.

**(1 Mark) (CBSE 2025 - 65/2/1)**

- A. Both Assertion (A) and Reason (R) are true and the Reason (R) is the correct explanation of the Assertion (A).
- B. Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).
- C. Assertion (A) is true but Reason (R) is false.
- D. Assertion (A) is false but Reason (R) is true.

Q.7 For a Linear Programming Problem (LPP), the given objective function

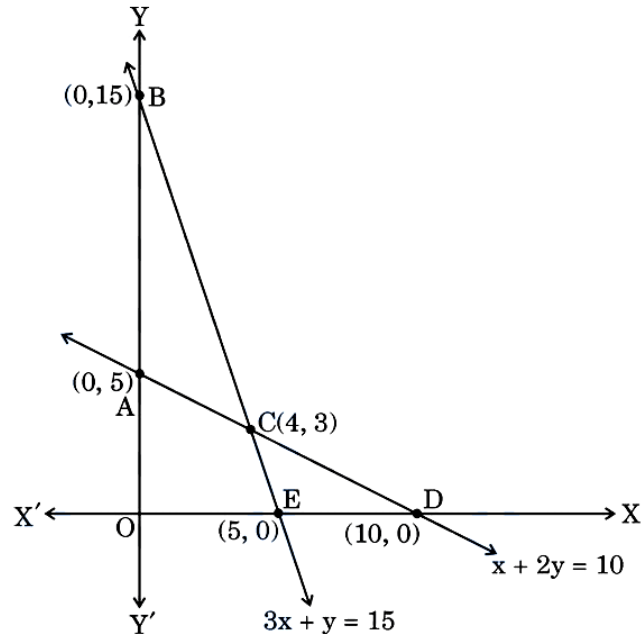
$$Z = 3x + 2y$$

is subject to constraints :

$$x + 2y \leq 10$$

$$3x + y \leq 15$$

$$x, y \geq 0$$

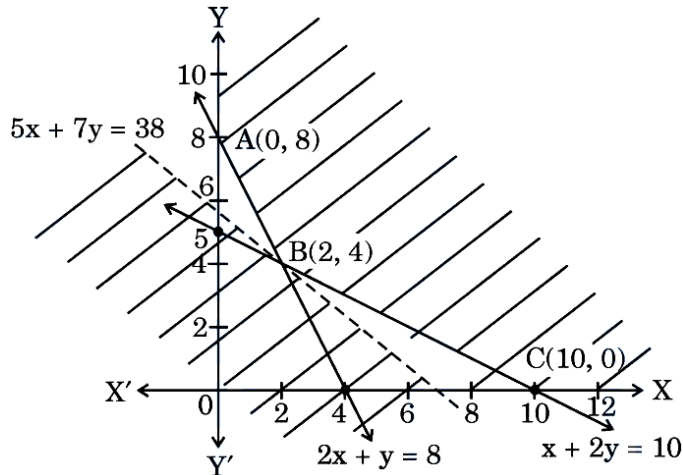


The correct feasible region is : (1 Mark) (CBSE 2025 - 65/2/1)

- A. CED
- B. Open unbounded region BCD
- C. ABC
- D. AOEC

Q.8 Assertion (A) : The shaded portion of the graph represents the feasible region for the given Linear Programming Problem (LPP).

(1 Mark) (CBSE 2025 - 65/5/1)



$$\text{Min } Z = 50x + 70y$$

subject to constraints

$$2x + y \geq 8, x + 2y \geq 10, x, y \geq 0$$

$$Z = 50x + 70y \text{ has a minimum value} = 380 \text{ at } B(2, 4).$$

Reason

(R)

: The region representing

$$50x + 70y < 380$$

does not have any point common with the feasible region.

A. Assertion (A) is false, but Reason (R) is true.

B. Assertion (A) is true, but Reason (R) is false.

C. Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).

D. Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A).

**Q.9** The corner points of the feasible region in graphical representation of a L.P.P. are  $(2,72)$ ,  $(15,20)$  and  $(40,15)$ . If  $Z=18x+9y$  be the objective function, then (1 Mark) (CBSE 2025 - 65/1/1)

A. Z is maximum at  $(2,72)$ , minimum at  $(15,20)$

B. Z is maximum at (15,20) minimum at (40,15)

C. Z is maximum at (40,15), minimum at (2,72)

D. Z is maximum at (40,15), minimum at (15,20)

**Q.10 If the feasible region of a linear programming problem with objective function  $Z=ax+ by$ , is bounded, then which of the following is correct ?**

(1 Mark) (CBSE 2025 - 65/1/1)

A. It will have both maximum and minimum values.

B. It will only have a minimum value.

C. It will only have a maximum value.

D. It will have neither maximum nor minimum value.

**Q.11 In a Linear Programming Problem, the objective function  $Z=5x+4y$  needs to be maximised under constraints  $3x+y\leq 6$ ,  $x\leq 1$ ,  $x, y\geq 0$ . Express the LPP on the graph and shade the feasible region and mark the corner points.**

(2 Mark) (CBSE 2025 - 65/7/1)

**Q.12 Solve the following Linear Programming Problem using graphical method :**

Maximise

$$Z = 100x + 50y$$

subject to the constraints

(3 Mark) (CBSE 2025 - 65/4/1)

$$3x + y \leq 600$$

$$x + y \leq 300$$

$$y \leq x + 200$$

$$x \geq 0, y \geq 0$$

**Q.13 Consider the Linear Programming Problem, where the objective function**

$$Z = (x + 4y)$$

**needs to be minimized subject to constraints**

$$2x + y \geq 1000$$

$$x + 2y \geq 800$$

$$x, y \geq 0$$

(3 Mark) (CBSE 2025 - 65/6/1)

Draw a neat graph of the feasible region and find the minimum value of Z.

Q.14 Solve the following linear programming problem graphically :

Minimise

$$Z = x - 5y$$

subject to the constraints :

(3 Mark) (CBSE 2025 - 65/2/1)

$$x - y \geq 0$$

$$-x + 2y \geq 2$$

$$x \geq 3, y \leq 4, y \geq 0$$

Q.15 In the Linear Programming Problem for objective function

$$Z = 18x + 10y$$

subject to constraints

(3 Mark) (CBSE 2025 - 65/7/1)

$$4x + y \geq 20$$

$$2x + 3y \geq 30$$

$$x, y \geq 0$$

find the minimum value of : Z

Q.16 In the Linear Programming Problem (LPP), find the point/points giving maximum value for

$$Z = 5x + 10y$$

subject to constraints

(3 Mark) (CBSE 2025 - 65/5/1)

$$x + 2y \leq 120$$

$$x + y \geq 60$$

$$x - 2y \geq 0$$

$$x, y \geq 0$$

**Q.17 Solve the following linear programming problem graphically :**

Maximise

$$Z = x + 2y$$

**Subject to the constraints :**

**(3 Mark) (CBSE 2025 - 65/1/1)**

$$x - y \geq 0$$

$$x - 2y \geq -2$$

$$x \geq 0, y \geq 0$$

## Answer

Q.1 B.  $3a = 2b$

Q.2 C. Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).

Q.3. C.

Z is minimum at S  $\left(\frac{18}{7}, \frac{2}{7}\right)$

Q.4. C. does not exist.

Q.5. C. The objective function maximizes the combined profit earned from selling X and Y.

Q.6. D. Assertion (A) is false but Reason (R) is true.

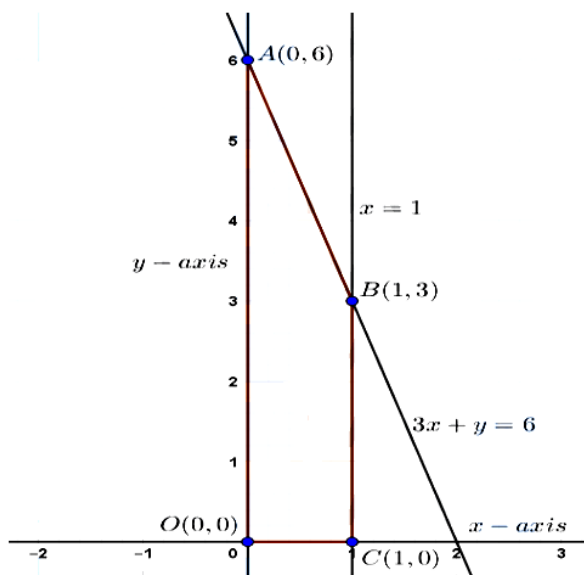
Q.7. D. AOEC

Q.8. D. Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A).

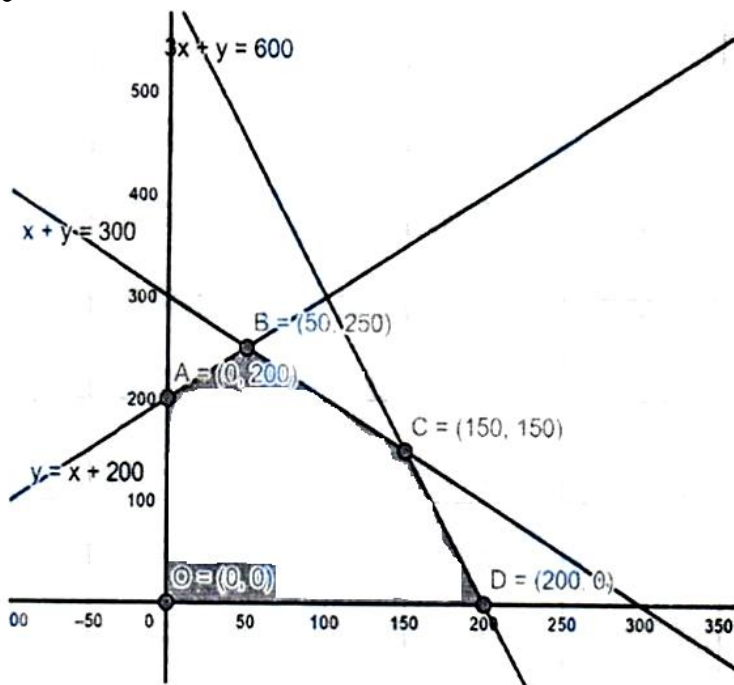
Q.9. D. Z is maximum at (40,15), minimum at (15,20)

Q.10. A. It will have both maximum and minimum values.

Q.11.



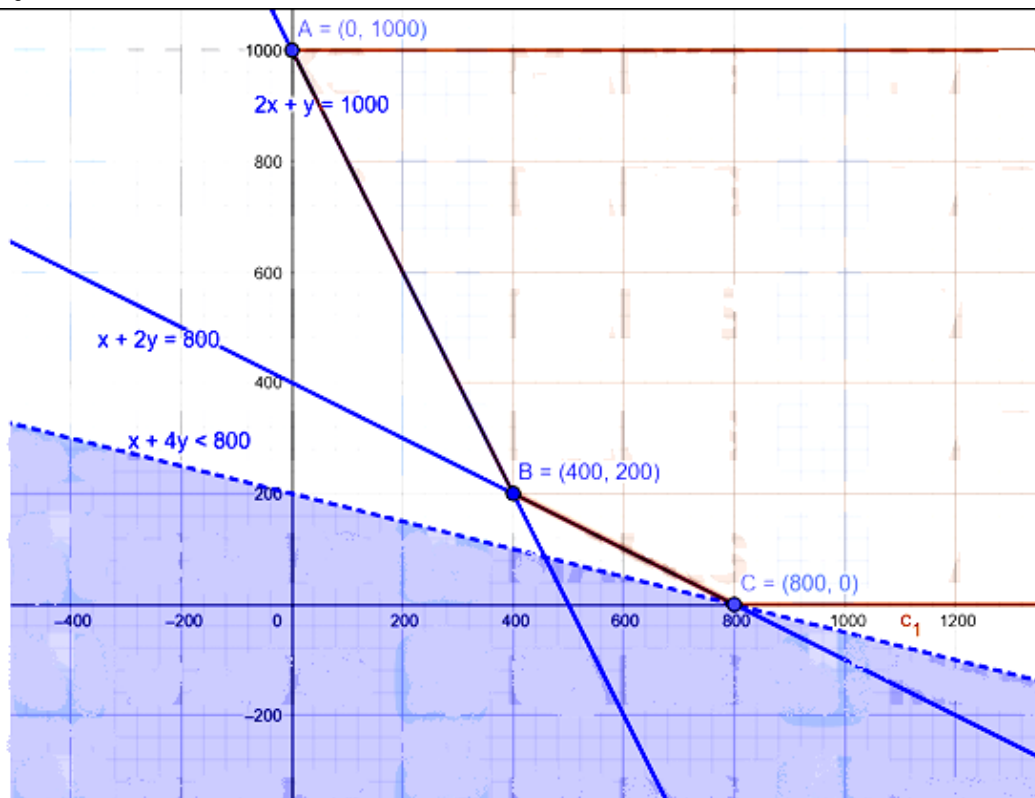
Q.12.



Corner Points	Value of $Z=100x+50y$
O (0,0)	0
A (0,200)	10000
B (50,250)	17500
C (150,150)	22500
D (200,0)	20000

$Z_{\max}=22500$  when  $x=150$ ,  $y=150$

Q.13.



Corner points

(800, 0)

(400, 200)

(0, 1000)

Val

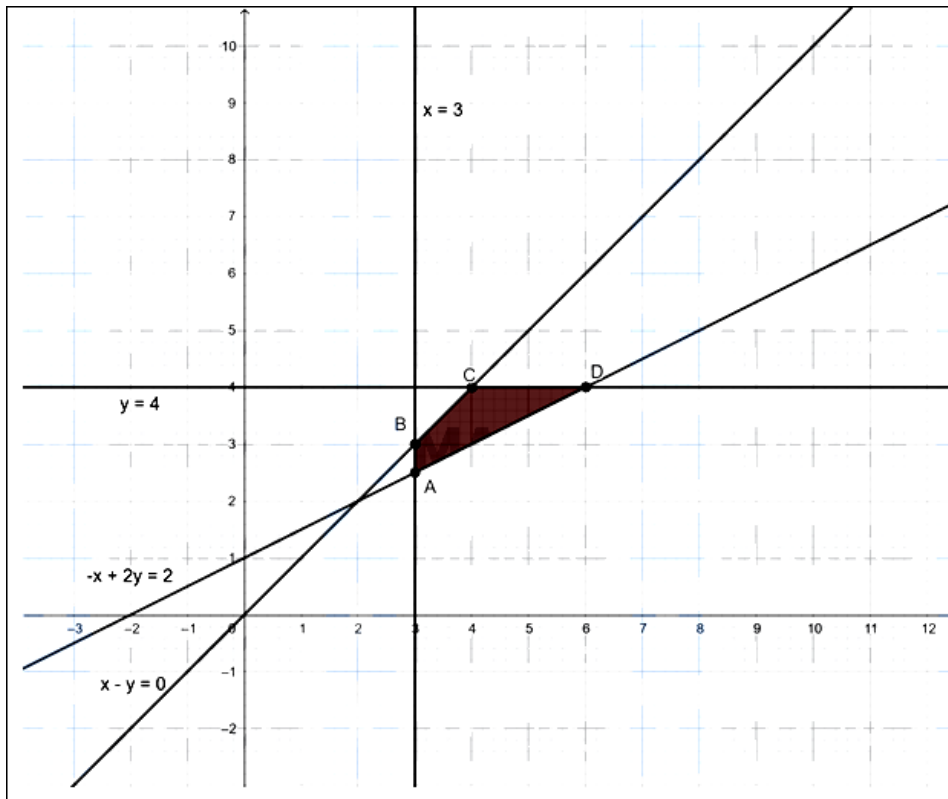
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$x + 4y < 800$  has no region common with feasible region, hence 800 is minimum

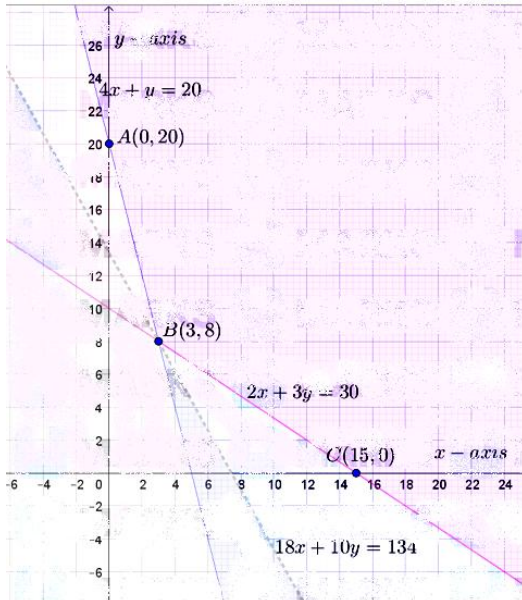
Q.14.



Corner Points	Value of $Z = x - 5y$
A(3, 2.5)	-9.5
B(3, 3)	-12
C(4, 4)	-16
D(6, 4)	-14

The minimum value of  $Z$  is -16, which is attained at  $x=4, y=4$ .

**Q.15.**

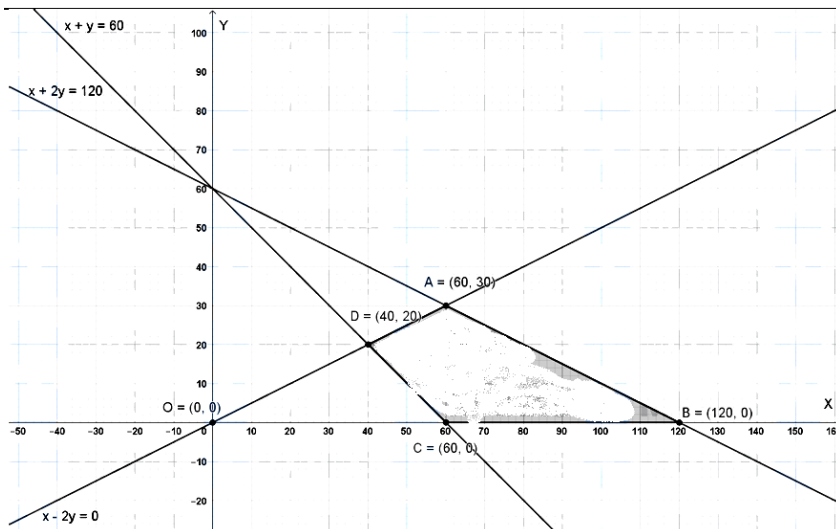


**Corner Points Value of  $Z = 18x + 10y$**

$A(0, 20)$	200
$B(3, 8)$	134
$C(15, 0)$	270

Also,  $Z < 134$ , does not have any common point with the feasible region,  
 $\therefore \text{Min}(Z) = 134$  at  $B(3, 8)$

**Q.16.**

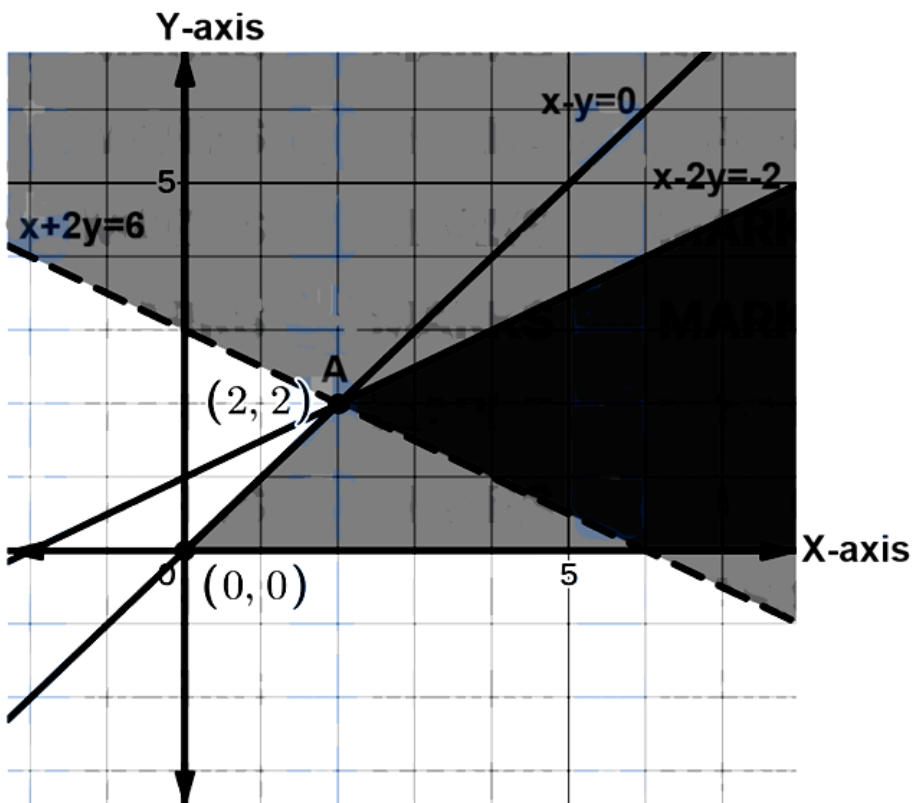


Corner Points	Value of Z
A (60,30)	600
B (120,0)	600
C (60,0)	300
D (40,20)	400

Since Z is maximum on points A and B

Hence all points lying on segment AB give maximum Z.

Q.17.



Corner Point	$Z=x+2y$
O (0,0)	0
A (2,2)	6

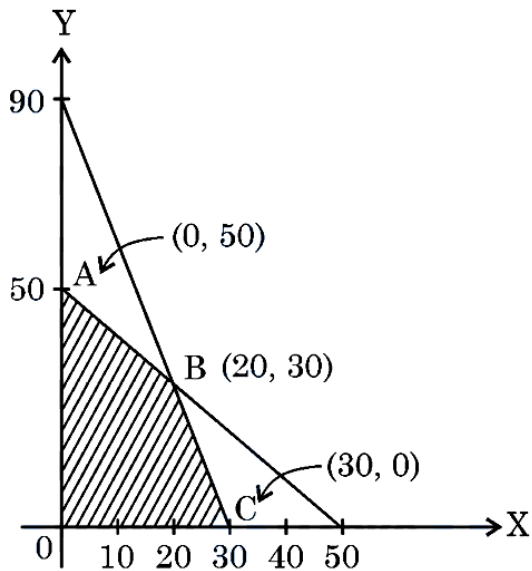
Since feasible region is unbounded. Plot  $x+2y>6$  which has common region with feasible region, thus Z has no maximum value.

**(2024)**

**Q.1 The common region determined by all the constraints of a linear programming problem is called : (1 Mark) (CBSE 2024 - 65/2/1)**

- A. an unbounded region
- B. a feasible region
- C. a bounded region
- D. an optimal region

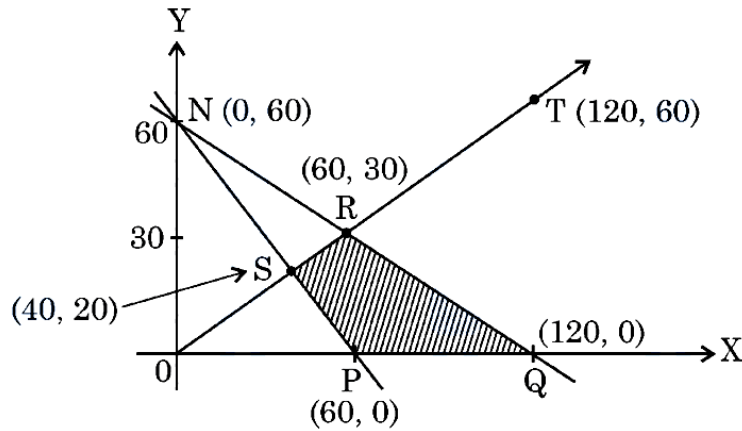
**Q.2 The maximum value of  $Z=4x+y$  for a L.P.P. whose feasible region is given below is : (1 Mark) (CBSE 2024 - 65/4/1)**



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- A. 50
- B. 110
- C. 120
- D. 170

**Q.3 Assertion (A) :** The corner points of the bounded feasible region of a L.P.P. are shown below. The maximum value of  $Z=x+2y$  occurs at infinite points.



**Reason (R) :** The optimal solution of a LPP having bounded feasible region must occur at corner points. **(1 Mark) (CBSE 2024 - 65/4/1)**

A. Both Assertion (A) and Reason (R) are true and the Reason (R) is the correct explanation of Assertion (A).

B. Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of the Assertion (A).

C. Assertion (A) is true, but Reason (R) is false.

D. Assertion (A) is false, but Reason (R) is true.

**Q.4 A linear programming problem deals with the optimization of a/an :**

A. quadratic function

B. logarithmic function

C. exponential function **(1 Mark) (CBSE 2024 - 65/1/1)**

D. linear function

**Q.5 The number of corner points of the feasible region determined by constraints  $x \geq 0, y \geq 0, x+y \geq 4$  is :** **(1 Mark) (CBSE 2024 - 65/1/1)**

A. 2

B. 0

C. 3

D. 1

Q.6 The restrictions imposed on decision variables involved in an objective function of a linear programming problem are called :

(1 Mark) (CBSE 2024 - 65/3/1)

A. optimal solutions

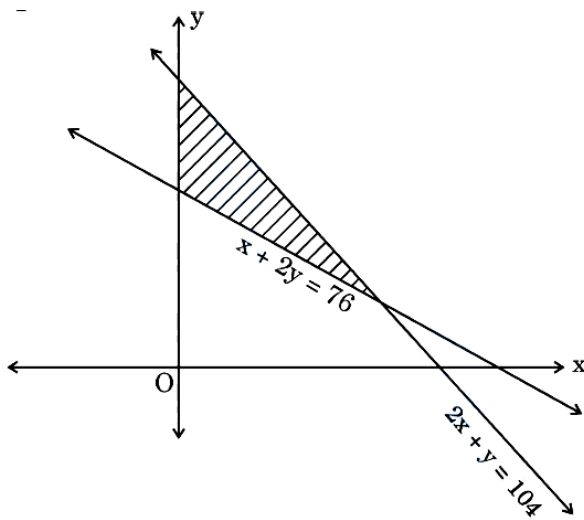
B. constraints

C. infeasible solutions

D. feasible solutions

Q.7 Of the following, which group of constraints represents the feasible region given below ?

(1 Mark) (CBSE 2024 - 65/3/1)



A.  $x+2y \leq 76, 2x+y \geq 104, x, y \geq 0$

B.  $x+2y \geq 76, 2x+y \leq 104, x, y \geq 0$

C.  $x+2y \geq 76, 2x+y \geq 104, x, y \geq 0$

D.  $x+2y \leq 76, 2x+y \leq 104, x, y \geq 0$

**Q.8 Solve the following linear programming problem graphically :**

Maximise

$$Z = 2x + 3y$$

subject to the constraints :

(3 Mark) (CBSE 2024 - 65/4/1)

$$x + y \leq 6$$

$$x \geq 2$$

$$y \leq 3$$

$$x, y \geq 0$$

**Q.9 Solve the following linear programming problem graphically :**

Maximise

$$z = 500x + 300y$$

, subject to constraints

(3 Mark) (CBSE 2024 - 65/1/1)

$$x + 2y \leq 12$$

$$2x + y \leq 12$$

$$4x + 5y \geq 20$$

$$x \geq 0, y \geq 0$$

**Q.10 Solve the following linear programming problem graphically :**

Maximise

$$z = 4x + 3y$$

, subject to the constraints

(3 Mark) (CBSE 2024 - 65/3/1)

$$x + y \leq 800$$

$$2x + y \leq 1000$$

$$x \leq 400$$

$$x, y \geq 0$$

**Q.11 The month of September is celebrated as the Rashtriya Poshan Maah across the country. Following a healthy and well-balanced diet is crucial in order to supply the body with the proper nutrients it needs. A balanced diet**

also keeps us mentally fit and promotes improved level of energy.

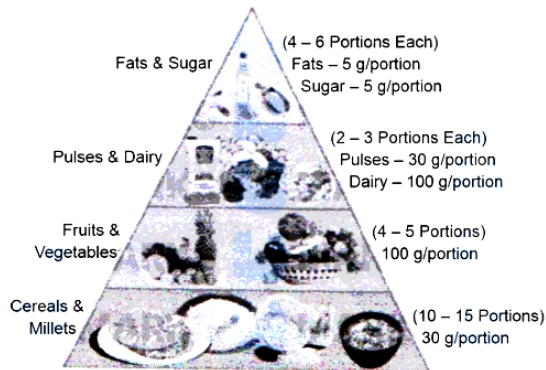


Figure-1

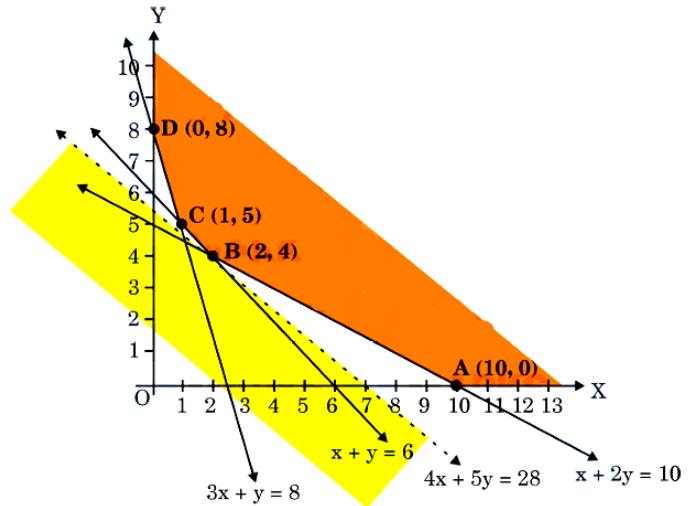


Figure-2

A dietician wishes to minimize the cost of a diet involving two types of foods, food X(xkg) and food Y(ykg) which are available at the rate of ₹16/kg and ₹20/kg respectively. The feasible region satisfying the constraints is shown in Figure-2.

On the basis of the above information, answer the following questions :

- (i) Identify and write all the constraints which determine the given feasible region in Figure-2.
- (ii) If the objective is to minimize cost  $Z=16x+20y$ , find the values of x and y at which cost is minimum. Also, find minimum cost assuming that minimum cost is possible for the given unbounded region.

(4 Mark) (CBSE 2024 - 65/2/1)

Q.12 Solve the following L.P.P. graphically :

$$\text{Maximise} \\ Z = 60x + 40y$$

Subject to

$$x + 2y \leq 12$$

$$2x + y \leq 12$$

$$4x + 5y \geq 20$$

$$x, y \geq 0$$

(5 Mark) (CBSE 2024 - 65/5/1)

## Answer

Q.1. B. a feasible region

Q.2. C. 120

Q.3. B. Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of the Assertion (A).

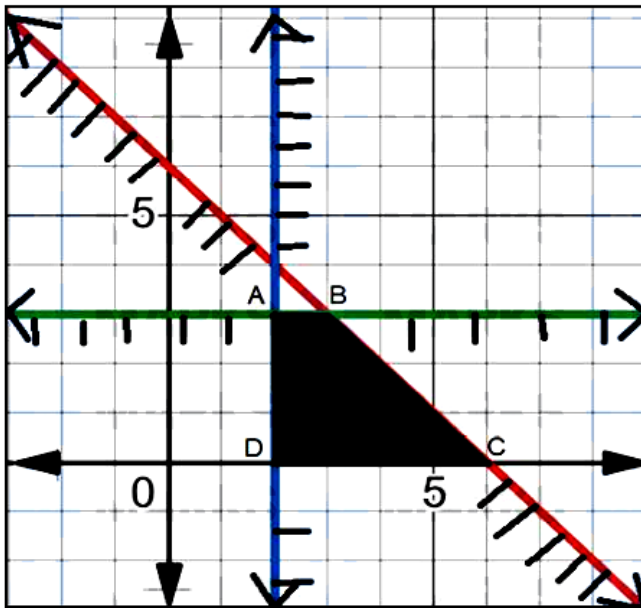
Q.4. D. linear function

Q.5. A. 2

Q.6. B. constraints

Q.7. B.  $x+2y \geq 76, 2x+y \leq 104, x, y \geq 0$

Q.8. On plotting the graph of  $x+y \leq 6, x \geq 2, y \leq 3, x \geq 0, y \geq 0$  we get the following graph and common shaded region is the region ABCD.



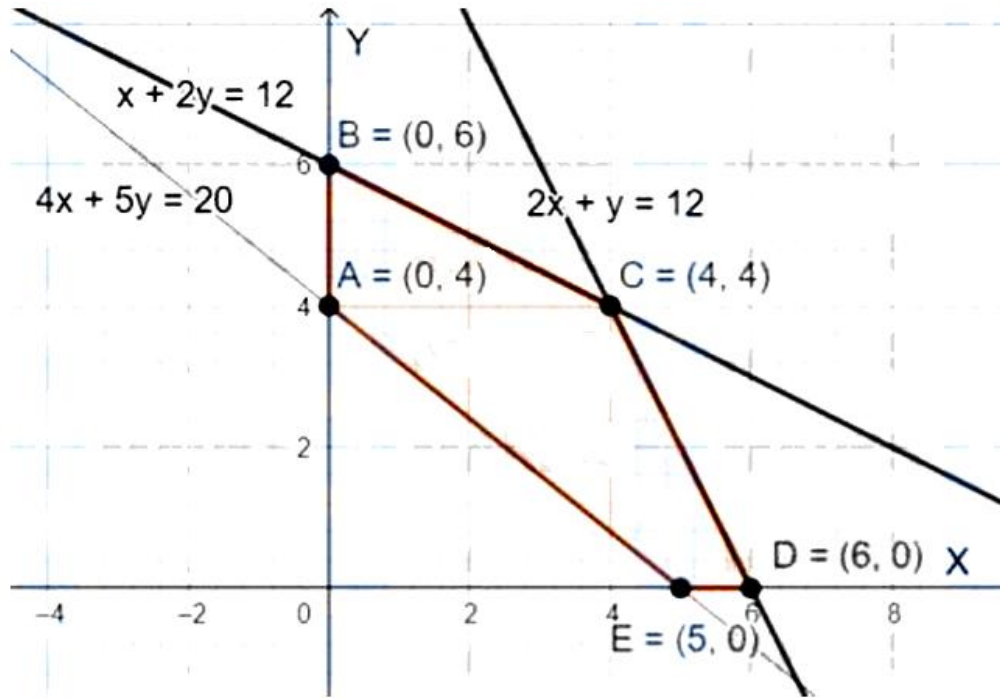
Now, Corner points of the common shaded region are A(2,3), B(3,3), C(6,0) & D(2,0). Thus,

Corner Points	Value of $Z=2x+3y$
A(2,3)	13

B(3,3)	15
C(6,0)	12
D(2,0)	4

So, Maximum Value of Z is 15 at  $x=3, y=3$ .

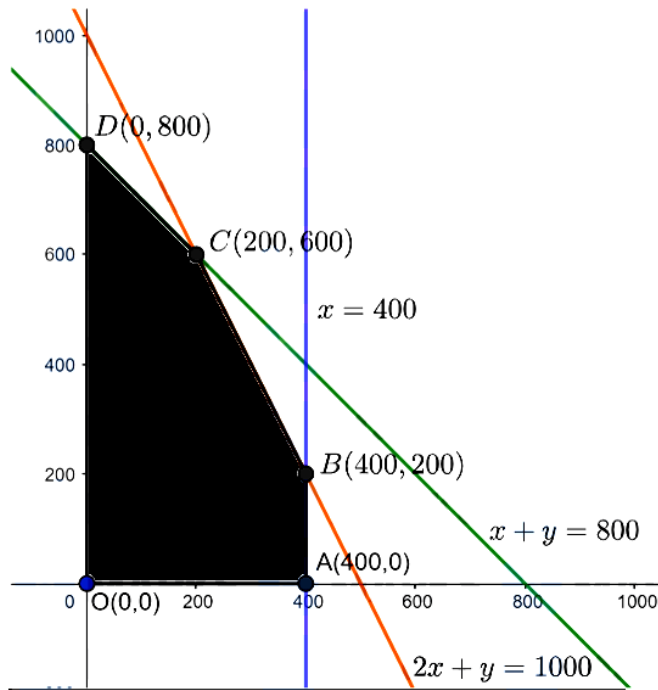
Q.9.  $\text{Max}z=500x+300y$



Corner Point	Z
A(0,4)	1200
B(0,6)	1800
C(4,4)	3200
D(6,0)	3000
E(5,0)	2500

$\text{Max}z=3200$  at  $x=4, y=4$

Q.10.



Corner Points	$z=4x+3y$
O(0,0)	0
A(400,0)	1600
B(400,200)	2200
C(200,600)	2600
D(0,800)	2400

$z_{\max}=2600$  when  $x=200, y=600$

Q.11.

(i) Constraints are

$$x + 2y \geq 10$$

$$x + y \geq 6$$

$$3x + y \geq 8$$

$$x \geq 0$$

$$y \geq 0$$

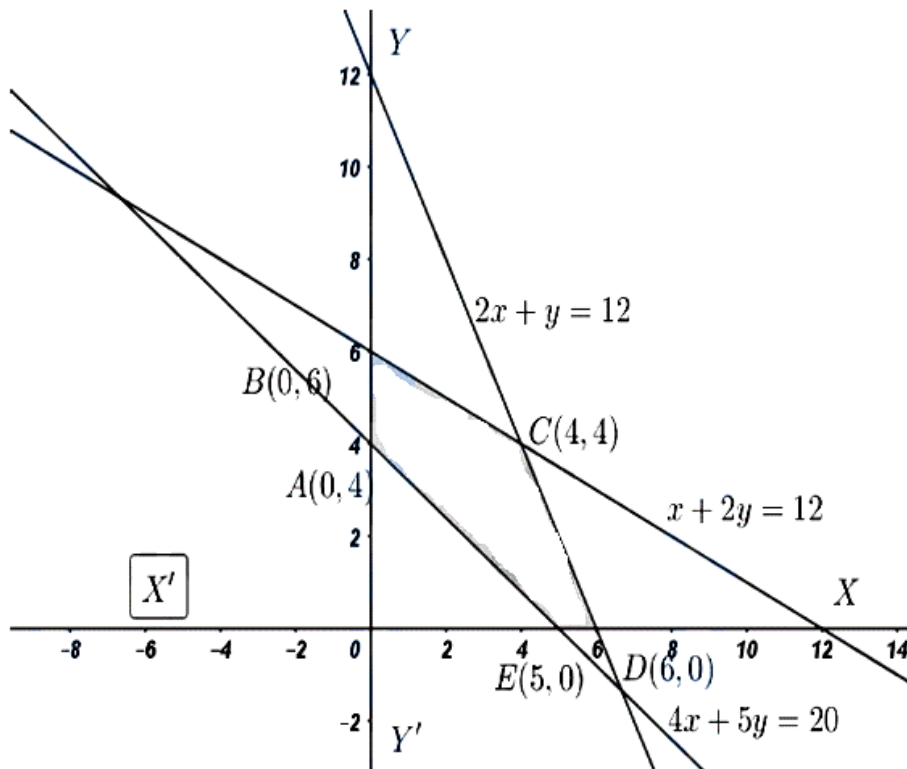
(ii)

Corner Points	$Z=16x+20y$
A(10,0)	160
B(2,4)	112
C(1,5)	116
D(0,8)	160

The minimum cost is :

₹ 112

Q.12.



Corner Points	Value of $Z=60x+40y$
A(0,4)	$Z=160$
B(0,6)	$Z=240$

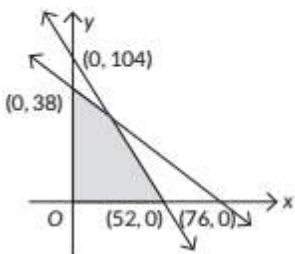
C(4,4)	Z=400
D(6,0)	Z=360
E(5,0)	Z=300

Max(Z)=400 at  $x=4,y=4$

## Previous Years' CBSE Board Questions

### 12.2 Linear Programming Problem and its Mathematical Formulation

#### MCQ

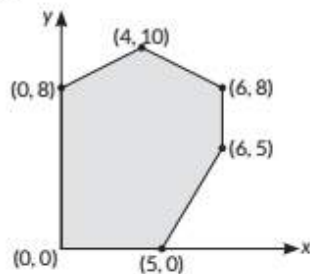
- Which of the following points satisfies both the inequations  $2x + y \leq 10$  and  $x + 2y \geq 8$ ?  
(a)  $(-2, 4)$  (b)  $(3, 2)$  (c)  $(-5, 6)$  (d)  $(4, 2)$   
(2023) U
- The solution set of the inequation  $3x + 5y < 7$  is  
(a) whole  $xy$ -plane except the points lying on the line  $3x + 5y = 7$ .  
(b) whole  $xy$ -plane along with the points lying on the line  $3x + 5y = 7$ .  
(c) open half plane containing the origin except the points of line  $3x + 5y = 7$ .  
(d) open half plane not containing the origin.  
(2023) U
- If the corner points of the feasible region of an LPP are  $(0, 3)$ ,  $(3, 2)$  and  $(0, 5)$ , then the minimum value of  $Z = 11x + 7y$  is  
(a) 21 (b) 33 (c) 14 (d) 35  
(Term I, 2021-22) Ev
- The number of solutions of the system of inequations  $x + 2y \leq 3$ ,  $3x + 4y \geq 12$ ,  $x \geq 0$ ,  $y \geq 1$  is  
(a) 0 (b) 2 (c) finite (d) infinite  
(Term I, 2021-22) U
- The maximum value of  $Z = 3x + 4y$  subject to the constraints  $x \geq 0$ ,  $y \geq 0$  and  $x + y \leq 1$  is  
(a) 7 (b) 4 (c) 3 (d) 10  
(Term I, 2021-22) Ev
- The feasible region of an LPP is given in the following figure  


Then, the constraints of the LPP are  $x \geq 0$ ,  $y \geq 0$  and  
(a)  $2x + y \leq 52$  and  $x + 2y \leq 76$   
(b)  $2x + y \leq 104$  and  $x + 2y \leq 76$   
(c)  $x + 2y \leq 104$  and  $2x + y \leq 76$   
(d)  $x + 2y \leq 104$  and  $2x + y \leq 38$   
(Term I, 2021-22) Ap
- If the minimum value of an objective function  $Z = ax + by$  occurs at two points  $(3, 4)$  and  $(4, 3)$  then  
(a)  $a + b = 0$  (b)  $a = b$   
(c)  $3a = b$  (d)  $a = 3b$   
(Term I, 2021-22) U
- For the following LPP, maximise  $Z = 3x + 4y$  subject to constraints  $x - y \geq -1$ ,  $x \leq 3$ ,  $x \geq 0$ ,  $y \geq 0$

the maximum value is

- (a) 0 (b) 4 (c) 25 (d) 30  
(Term I, 2021-22) Ap

- The corner points of the feasible region determined by the system of linear inequalities are  $(0, 0)$ ,  $(4, 0)$ ,  $(2, 4)$  and  $(0, 5)$ . If the maximum value of  $z = ax + by$ , where  $a, b > 0$  occurs at both  $(2, 4)$  and  $(4, 0)$ , then  
(a)  $a = 2b$  (b)  $2a = b$   
(c)  $a = b$  (d)  $3a = b$  (2020) U
- In an LPP, if the objective function  $z = ax + by$  has the same maximum value on two corner points of the feasible region, then the number of points at which  $z_{\max}$  occurs is  
(a) 0 (b) 2 (c) finite (d) infinite  
(2020) U
- The feasible region for an LPP is shown below :  
Let  $z = 3x - 4y$  be the objective function. Minimum of  $z$  occurs at



- (a)  $(0, 0)$  (b)  $(0, 8)$   
(c)  $(5, 0)$  (d)  $(4, 10)$   
(NCERT Exemplar, 2020) Ap

- The graph of the inequality  $2x + 3y > 6$  is  
(a) half plane that contains the origin  
(b) half plane that neither contains the origin nor the points of the line  $2x + 3y = 6$ .  
(c) whole  $XOY$ -plane excluding the points on the line  $2x + 3y = 6$ .  
(d) entire  $XOY$ -plane. (2020) U
- The objective function of an LPP is  
(a) a constant  
(b) a linear function to be optimised  
(c) an inequality  
(d) a quadratic expression (2020) R

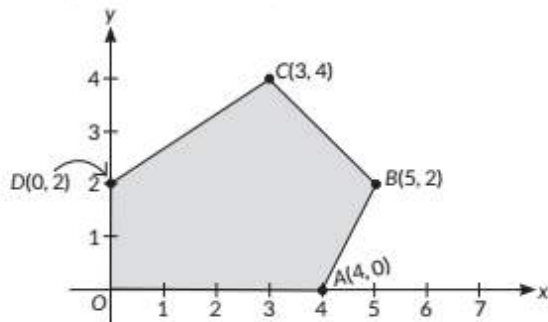
#### SA II (3 marks)

- Solve the following linear programming problem graphically:  
Maximise  $z = -3x - 5y$   
Subject to the constraints  
 $-2x + y \leq 4$   
 $x + y \geq 3$   
 $x - 2y \leq 2$ ,  
 $x \geq 0, y \geq 0$ .  
(2023) Ev

**LA I (4 marks)**

15. Solve the following linear programming problem graphically:  
 Maximize  $z = 3x + 9y$   
 Subject to constraints  
 $x + 3y \leq 60$   
 $x + y \geq 10$   
 $x \leq y$   
 $x, y \geq 0$  (2021) (Ev)

16. The corner points of the feasible region determined by the system of linear inequations are as shown below:



Answer each of the following :

- (i) Let  $z = 13x - 15y$  be the objective function. Find the maximum and minimum values of  $z$  and also the corresponding points at which the maximum and minimum values occur.  
 (ii) Let  $z = kx + y$  be the objective function. Find  $k$ , if the value of  $z$  at A is same as the value of  $z$  at B. (2021)
17. Solve the following LPP graphically :  
 Minimize  $z = 5x + 7y$   
 Subject to the constraints  
 $2x + y \geq 8, x + 2y \geq 10, x, y \geq 0$  (2020) (Ev)

18. Solve the following LPP graphically :  
 Minimise  $Z = 5x + 10y$   
 Subject to constraints  $x + 2y \leq 120, x + y \geq 60,$   
 $x - 2y \geq 0$  and  $x, y \geq 0$   
 (NCERT Exemplar, Delhi 2017) (Ev)
19. Maximise  $Z = x + 2y$   
 Subject to the constraints:  
 $x + 2y \geq 100, 2x - y < 0, 2x + y \leq 200, x, y \geq 0$   
 Solve the above LPP graphically.  
 (NCERT, AI 2017) (Ev)

**LA II (5 / 6 marks)**

20. Solve the following linear programming problem graphically.  
 Maximize :  $P = 70x + 40y$   
 Subject to :  $3x + 2y \leq 9, 3x + y \leq 9, x \geq 0, y \geq 0.$  (2023) (Ev)
21. Solve the following linear programming problem graphically.  
 Minimize :  $Z = 60x + 80y$   
 Subject to constraints:  
 $3x + 4y \geq 8$   
 $5x + 2y \geq 11$   
 $x, y \geq 0$  (2023) (Cr)
22. Find graphically, the maximum value of  $z = 2x + 5y$ , subject to constraints given below:  
 $2x + 4y \leq 8, 3x + y \leq 6, x + y \leq 4; x \geq 0, y \geq 0$   
 (Delhi 2015) (Ev)
23. Maximise  $z = 8x + 9y$  subject to the constraints given below :  
 $2x + 3y \leq 6, 3x - 2y \leq 6, y \leq 1; x, y \geq 0$   
 (Foreign 2015) (Ev)

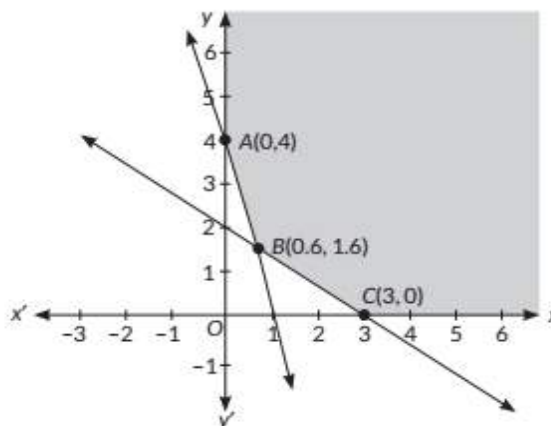
**CBSE Sample Questions**

**12.2 Linear Programming Problem and its Mathematical Formulation**

**MCQ**

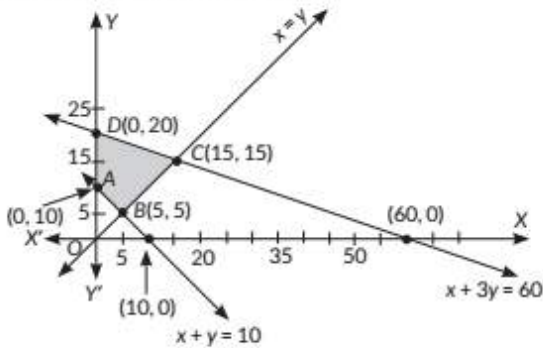
1. The solution set of the inequality  $3x + 5y < 4$  is  
 (a) an open half-plane not containing the origin.  
 (b) an open half-plane containing the origin.  
 (c) the whole XY-plane not containing the line  $3x + 5y = 4.$   
 (d) a closed half plane containing the origin. (2022-23) (Ev)
2. The corner points of the shaded unbounded feasible region of an LPP are  $(0, 4), (0.6, 1.6)$  and  $(3, 0)$  as shown in the figure. The minimum value of the

objective function  $Z = 4x + 6y$  occurs at



- (a) (0.6, 1.6) only
- (b) (3, 0) only
- (c) (0.6, 1.6) and (3, 0) only
- (d) at every point of the line-segment joining the points (0.6, 1.6) and (3, 0) (2022-23) (Ev)

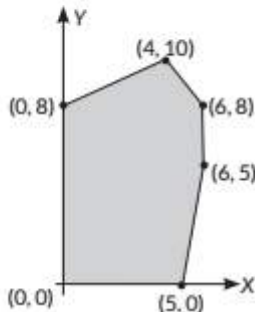
3. Based on the given shaded region as the feasible region in the graph, at which point(s) is the objective function  $Z = 3x + 9y$  maximum?



- (a) Point B
- (b) Point C
- (c) Point D
- (d) every point on the line segment CD

(Term I, 2021-22) (U)

4. In the given graph, the feasible region for a LPP is shaded. The objective function  $Z = 2x - 3y$ , will be minimum at



- (a) (4, 10)
- (b) (6, 8)
- (c) (0, 8)
- (d) (6, 5)

(Term I, 2021-22) (Ap)

5. A linear programming problem is as follows :

Minimize  $Z = 30x + 50y$   
 Subject to the constraints,  
 $3x + 5y \geq 15$   
 $2x + 3y \leq 18$   
 $x \geq 0, y \geq 0$

In the feasible region, the minimum value of  $Z$  occurs at

- (a) a unique point
- (b) no point
- (c) infinitely many points
- (d) two points only

(Term I, 2021-22) (U)

6. For an objective function  $Z = ax + by$ , where  $a, b > 0$ ; the corner points of the feasible region determined by a set of constraints (linear inequalities) are (0, 20), (10, 10), (30, 30) and (0, 40). The condition on

$a$  and  $b$  such that the maximum  $Z$  occurs at both the points (30, 30) and (0, 40) is

- (a)  $b - 3a = 0$
- (b)  $a = 3b$
- (c)  $a + 2b = 0$
- (d)  $2a - b = 0$

(Term I, 2021-22)

7. In a linear programming problem, the constraints on the decision variables  $x$  and  $y$  are  $x - 3y \geq 0, y \geq 0, 0 \leq x \leq 3$ . The feasible region

- (a) is not in the first quadrant
- (b) is bounded in the first quadrant
- (c) is unbounded in the first quadrant
- (d) does not exist

(Term I, 2021-22) (U)

#### SA II (3 marks)

8. Solve the following Linear Programming Problem graphically:

Maximize  $Z = 400x + 300y$  subject to  $x + y \leq 200$ ,  
 $x \leq 40, x \geq 20, y \geq 0$  (2022-23) (Ev)

#### LA II (5/6 marks)

9. Solve the following linear programming problem (L.P.P) graphically.

Maximize  $Z = 3x + y$   
 Subject to constraints;

$$x + 2y \geq 100$$

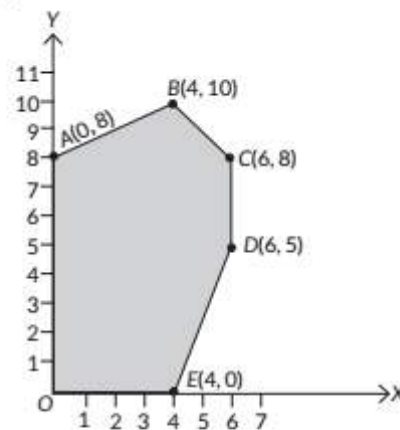
$$2x - y \leq 0$$

$$2x + y \leq 200$$

$$x, y \geq 0$$

(2020-21) (Ap)

10. The corner points of the feasible region determined by the system of linear constraints are as shown below:



Answer each of the following:

(i) Let  $Z = 3x - 4y$  be the objective function. Find the maximum and minimum value of  $Z$  and also the corresponding points at which the maximum and minimum value occurs.

(ii) Let  $Z = px + qy$ , where  $p, q > 0$  be the objective function. Find the condition on  $p$  and  $q$  so that the maximum value of  $Z$  occurs at  $B(4, 10)$  and  $C(6, 8)$ . Also mention the number of optimal solutions in this case. (2020-21) (Ev)

# Detailed SOLUTIONS

## Previous Years' CBSE Board Questions

1. (d): We have,  $2x + y \leq 10$  and  $x + 2y \geq 8$   
Let us check which of the given points satisfy the given inequation one by one.

(a)  $(-2, 4)$

$$2 \times (-2) + 4 = -4 + 4 = 0 \leq 10$$

and  $-2 + 2 \times 4 = -2 + 8 = 6 \not\geq 8$

(b)  $(3, 2)$

$$2 \times 3 + 2 = 6 + 2 = 8 \leq 10$$

$$3 + 2 \times 2 = 3 + 4 = 7 \not\geq 8$$

(c)  $(-5, 6)$

$$2 \times (-5) + 6 = -10 + 6 = -4 \leq 10$$

$$-5 + 2 \times 6 = -5 + 12 = 7 \not\geq 8$$

(d)  $(4, 2)$

$$2 \times 4 + 2 = 10 \leq 10; 4 + 2 \times 2 = 8 \geq 8$$

$\therefore (4, 2)$  satisfy both the inequations.

2. (c): Given inequation is  $3x + 5y < 7$

Let us draw the graph of  $3x + 5y = 7$

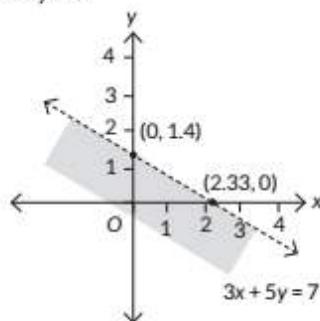
x	0	2.33
y	1.4	0

Substitute,  $x = 0$  and  $y = 0$  in the inequation, we get

$$3(0) + 5(0) < 7$$

i.e.,  $0 < 7$  which is true.

$\therefore$  The solution set of the inequality is an open half plane containing the origin except the points on line  $3x + 5y = 7$ .



3. (a): Given,  $Z = 11x + 7y$

$$\text{At } (0, 3), Z = 11 \times 0 + 7 \times 3 = 21$$

$$\text{At } (3, 2), Z = 11 \times 3 + 7 \times 2 = 47$$

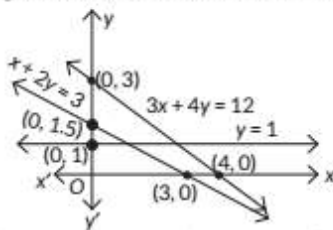
$$\text{At } (0, 5), Z = 11 \times 0 + 7 \times 5 = 35$$

Thus,  $Z$  is minimum at  $(0, 3)$  and minimum value of  $Z$  is 21.

4. (a): Given,

$$x + 2y \leq 3, 3x + 4y \geq 12, x \geq 0, y \geq 1$$

The graph of given constraints is shown here.

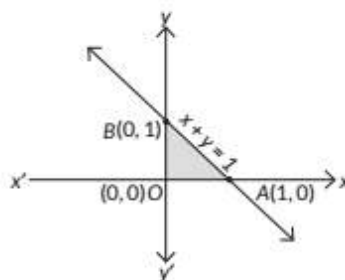


Since, there is no common region, so, no solution exists.

### Key Points

A feasible region is an area defined by a set of coordinates that satisfy a system of inequalities.

5. (b): We have to maximise  $Z = 3x + 4y$   
Subject to constraints,  $x \geq 0, y \geq 0$  and  $x + y \leq 1$



The shaded portion  $OAB$  is the feasible region, where  $O(0, 0)$ ,  $A(1, 0)$  and  $B(0, 1)$  are the corner points.

$$\text{At } O(0, 0), Z = 3 \times 0 + 4 \times 0 = 0$$

$$\text{At } A(1, 0), Z = 3 \times 1 + 4 \times 0 = 3$$

$$\text{At } B(0, 1), Z = 3 \times 0 + 4 \times 1 = 4$$

$\therefore$  Maximum value of  $Z$  is 4, which occurs at  $B(0, 1)$ .

### Concept Applied

Any point in the feasible region of a linear programming problem that gives the optimal value (maximum or minimum) of the objective function is called an optimal solution.

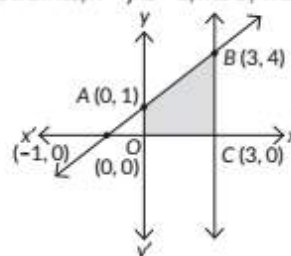
6. (b): Clearly, the pair of points given in graph, and  $(0, 104)$ ;  $(52, 0)$  and  $(0, 38)$ ;  $(76, 0)$  satisfy the corresponding equations given in option(b) i.e.,  $2x + y \leq 104$  and  $x + 2y \leq 76$ .

7. (b): Since, minimum value of  $Z = ax + by$  occurs at two points  $(3, 4)$  and  $(4, 3)$ .

$$\therefore 3a + 4b = 4a + 3b \Rightarrow a = b$$

8. (c): Given,  $Z = 3x + 4y$

Subject to constraints,  $x - y \geq -1, x \leq 3; x \geq 0, y \geq 0$



The shaded region  $OABC$  is the feasible region, where corner points are  $O(0, 0)$ ,  $A(0, 1)$ ,  $B(3, 4)$  and  $C(3, 0)$

$$\text{At } O(0, 0), Z = 3(0) + 4(0) = 0$$

$$\text{At } A(0, 1), Z = 3(0) + 4(1) = 4$$

$$\text{At } B(3, 4), Z = 3(3) + 4(4) = 25$$

$$\text{At } C(3, 0), Z = 3(3) + 4(0) = 9$$

$\therefore$  Maximum value of  $Z$  is 25, which occurs at  $B(3, 4)$ .

9. (a): Since, maximum value of  $z = ax + by$  occurs at both  $(2, 4)$  and  $(4, 0)$ .

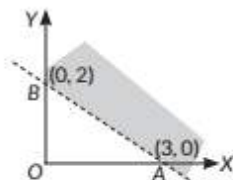
$$\therefore 2a + 4b = 4a + 0 \Rightarrow 4b = 2a \Rightarrow 2b = a$$

10. (d): In an LPP, if the objective function  $z = ax + by$  has the same maximum value on two corner points of the feasible region, then the number of points at which  $z_{\max}$  occurs is infinite.

11. (b) : We know that minimum of objective function occurs at corner points.

Corner points	Value of $z = 3x - 4y$
(0, 0)	0
(5, 0)	15
(6, 5)	-2
(6, 8)	-14
(4, 10)	-28
(0, 8)	-32 ← Minimum

12. (b) : From the graph of inequality  $2x + 3y > 6$ . It is clear that it does not contain the origin nor the points of the line  $2x + 3y = 6$ .

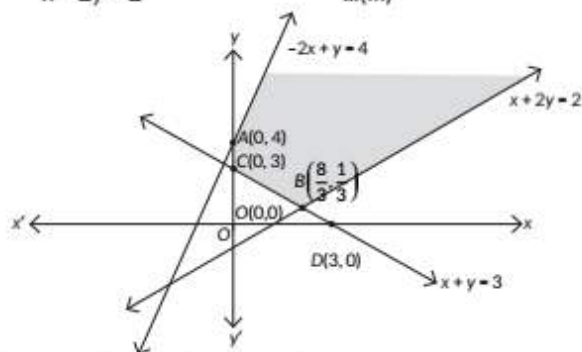


13. (b): A linear function to be optimized is called an objective function.

14. We have, maximise  $z = -3x - 5y$

Converting the given inequations into equations, we get

$$\begin{aligned} -2x + y &= 4 && \dots(i) \\ x + y &= 3 && \dots(ii) \\ x - 2y &= 2 && \dots(iii) \end{aligned}$$



We draw the graph of these lines.

As,  $x \geq 0, y \geq 0$  so the solution lies in first quadrant.

From graph, corner point of feasible region are  $A(0, 4)$ ,  $B(8/3, 1/3)$  and  $C(0, 3)$

The value of  $z$  at these corner points are shown as :

Corner points	$z = -3x - 5y$
$A(0, 4)$	-20
$B(8/3, 1/3)$	-29/3 ← Maximum
$C(0, 3)$	-15

Hence maximum value of  $z = \frac{-29}{3}$ .

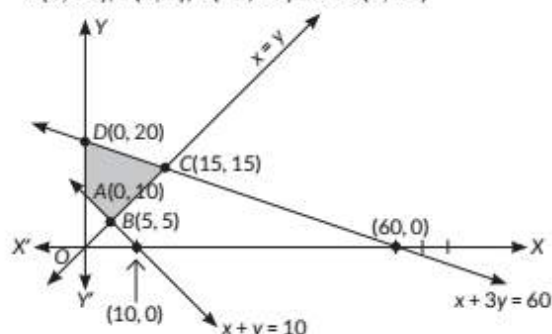
15. We have, maximize  $z = 3x + 9y$

Subject to constraints,  $x + 3y \leq 60, x + y \geq 10, x \leq y, x, y \geq 0$   
To solve L.P.P. graphically, we convert inequations into equations.

$l_1 : x + 3y = 60, l_2 : x + y = 10, l_3 : x = y, x = 0$  and  $y = 0$   
 $l_2$  and  $l_3$  intersect at (5, 5).  $l_1$  and  $l_3$  intersect at (15, 15).

The shaded region ABCD is the feasible region and is bounded. The corner points of the feasible region are

$A(0, 10), B(5, 5), C(15, 15)$  and  $D(0, 20)$



Corner Points	Value of $z = 3x + 9y$
$A(0, 10)$	90
$B(5, 5)$	60
$C(15, 15)$	180
$D(0, 20)$	180

Maximum (Multiple optimal solutions)

The maximum value of  $Z$  on the feasible region occurs at the two corner points  $C(15, 15)$  and  $D(0, 20)$  and it is 180 in each case.

16. (i)

Corner Points	$z = 13x - 15y$
$O(0, 0)$	0
$A(4, 0)$	52 (Maximum)
$B(5, 2)$	35
$C(3, 4)$	-21
$D(0, 2)$	-30 (Minimum)

Thus, maximum value of  $Z$  is 52 at  $A(4, 0)$  and minimum value of  $Z$  is -30 at  $D(0, 2)$

(ii) Since value of  $z = kx + y$  at  $A(4, 0)$  is same as the value of  $Z$  at  $B(5, 2)$ .

$$\therefore k \cdot 4 + 0 = k \cdot 5 + 2 \Rightarrow 4k = 5k + 2 \Rightarrow k = -2$$

17. We have, minimize  $z = 5x + 7y$ ,

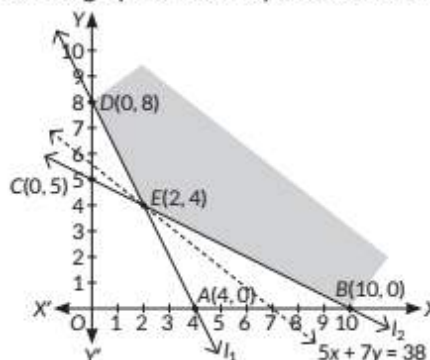
Subject to constraints,  $2x + y \geq 8, x + 2y \geq 10, x, y \geq 0$

To solve LPP graphically, we convert inequations into equations.

Now,  $l_1 : 2x + y = 8, l_2 : x + 2y = 10$  and  $x = 0, y = 0$

$l_1$  and  $l_2$  intersect at  $E(2, 4)$ .

Let us draw the graph of these equations as shown below.



The corner points of the feasible region are  $D(0, 8)$ ,  $B(10, 0)$  and  $E(2, 4)$ .

Corner points	Value of $z = 5x + 7y$
D (0, 8)	56
B (10, 0)	50
E (2, 4)	38 (Minimum)

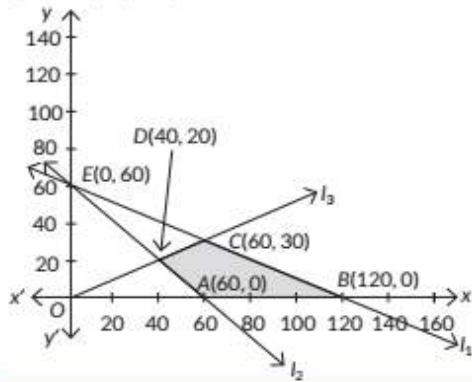
From the table, we find that 38 is the minimum value of  $z$  at  $E(2, 4)$ . Since the region is unbounded, so we draw the graph of inequality  $5x + 7y < 38$  to check whether the resulting open half plane has any point common with the feasible region. Since it has no point in common. So, the minimum value of  $z$  is obtained at  $E(2, 4)$  and the minimum value of  $z = 38$ .

### Answer Tips

→ If the region is unbounded, then a maximum or minimum value of the objective function may not exist. If it exists, it must occur at a corner point of region.

18. We have, Minimise  $Z = 5x + 10y$ ,  
Subject to constraints :

$x + 2y \leq 120$   
 $x + y \geq 60$   
 $x - 2y \geq 0$  and  $x, y \geq 0$   
 To solve L.P.P graphically, we convert inequations into equations.  
 $l_1 : x + 2y = 120$ ,  $l_2 : x + y = 60$ ,  $l_3 : x - 2y = 0$  and  $x = 0, y = 0$   
 $l_1$  and  $l_2$  intersect at  $E(0, 60)$ ,  $l_1$  and  $l_3$  intersect at  $C(60, 30)$ ,  
 $l_2$  and  $l_3$  intersect at  $D(40, 20)$ .  
 The shaded region ABCD is the feasible region and is bounded.  
 The corner points of the feasible region are  $A(60, 0)$ ,  $B(120, 0)$ ,  
 $C(60, 30)$  and  $D(40, 20)$ .



Corner points	Value of $Z = 5x + 10y$
A(60, 0)	300 ← (Minimum)
B(120, 0)	600
C(60, 30)	600
D(40, 20)	400

Hence,  $Z$  is minimum at  $A(60, 0)$  i.e., 300.

### Commonly Made Mistake

→ Remember to convert inequations into equations.

19. Maximise  $Z = x + 2y$ , Subject to constraints :  
 $x + 2y \geq 100$ ,  $2x - y < 0$ ,  $2x + y \leq 200$  and  $x, y \geq 0$ .  
 Converting the inequations into equations, we obtain the lines

$$\begin{aligned}
 l_1 : x + 2y &= 100 && \dots(i) \\
 l_2 : 2x - y &= 0 && \dots(ii) \\
 l_3 : 2x + y &= 200 && \dots(iii) \\
 l_4 : x &= 0 && \dots(iv) \\
 \text{and } l_5 : y &= 0 && \dots(v)
 \end{aligned}$$

By intercept form, we get

$$l_1 : \frac{x}{100} + \frac{y}{50} = 1$$

⇒ The line  $l_1$  meets the coordinate axes at (100, 0) and (0, 50).

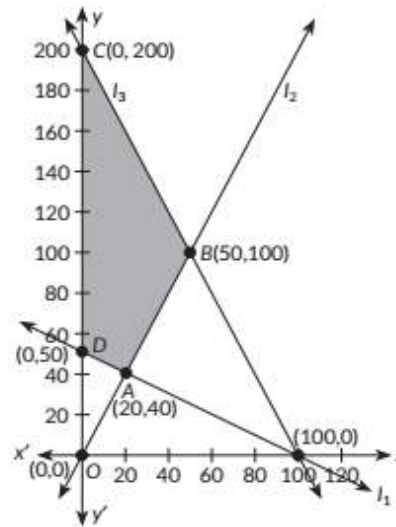
$$l_2 : 2x = y$$

⇒ The line  $l_2$  passes through origin and cuts  $l_1$  and  $l_3$  at (20, 40) and (50, 100) respectively.

$$l_3 : \frac{x}{100} + \frac{y}{200} = 1$$

⇒ The line  $l_3$  meets the coordinates axes at (100, 0) and (0, 200).

$l_4 : x = 0$  is the y-axis,  $l_5 : y = 0$  is the x-axis



Now, plotting the above points on the graph, we get the feasible region of the LPP as shaded region ABCD. The coordinates of the corner points of the feasible region ABCD are  $A(20, 40)$ ,  $B(50, 100)$ ,  $C(0, 200)$ ,  $D(0, 50)$ .

$$\text{Now, } Z_A = 20 + 2 \times 40 = 100$$

$$Z_B = 50 + 2 \times 100 = 250, Z_C = 0 + 2 \times 200 = 400$$

$$Z_D = 0 + 2 \times 50 = 100$$

∴  $Z$  is maximum at  $C(0, 200)$  and having value 400.

20. We have, maximize  $P = 70x + 40y$

Subject to :  $3x + 2y \leq 9$

$$3x + y \leq 9$$

$$x \geq 0, y \geq 0$$

Convert all inequations into equation, we get

$$3x + 2y = 9 \quad \dots (i)$$

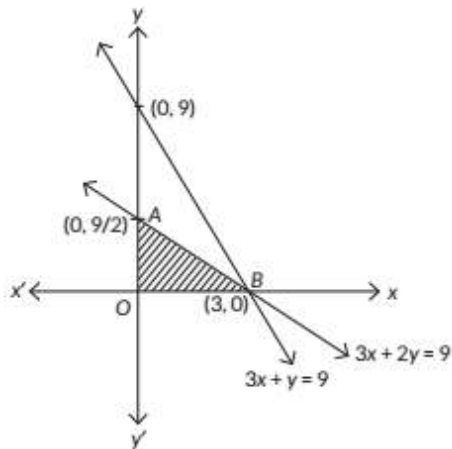
$$3x + y = 9 \quad \dots (ii)$$

$$x = 0 \text{ and } y = 0$$

Solving (i) and (ii), we get

$$x = 3, y = 0$$

So, point of intersection of equation (i) and (ii) are (3, 0).



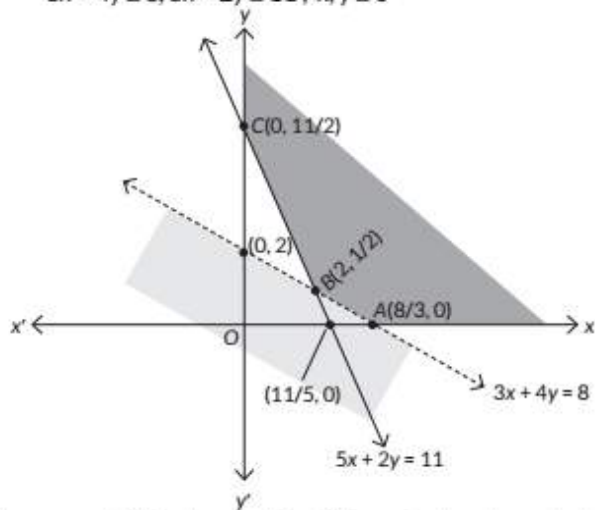
The given shaded region is the feasible region.  
The corner points of the feasible region are  $O(0, 0)$ ,  $A(0, 9/2)$  and  $B(3, 0)$ .

Corner points	Value of $p = 70x + 40y$
$O(0, 0)$	$70 \times 0 + 40 \times 0 = 0$
$A(0, 9/2)$	$70 \times 0 + 40 \times \frac{9}{2} = 180$
$B(3, 0)$	$70 \times 3 + 40 \times 0 = 210$ (maximum)

So,  $P$  is maximum at point  $B(3, 0)$ .

21. We have,  $\min z = 60x + 80y$ ;  
Subject to constraints;

$$3x + 4y \geq 8, 5x + 2y \geq 11; x, y \geq 0$$



From graph, it is clear that feasible region is unbounded.  
The corner points of the feasible region are  $A(8/3, 0)$ ,  $B(2, 1/2)$  and  $C(0, 11/2)$ .

The value of  $Z$  at these corner points are as follows:

Corner Points	$Z = 60x + 80y$
$A(8/3, 0)$	160
$B(2, 1/2)$	160
$C(0, 11/2)$	440

(Minimum)

As the feasible region is unbounded,

$\therefore$  160 may or may not be the minimum value of  $Z$ .

So, we graph the inequality  $60x + 80y < 160$  i.e.,  $3x + 4y < 8$

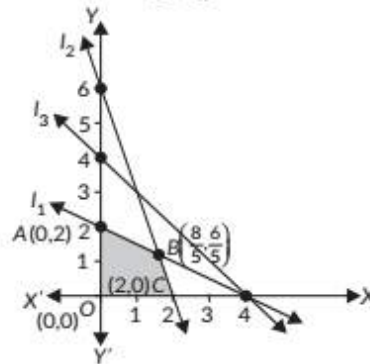
and check whether the resulting half plane has points in common with the feasible region or not.

From graph, it can be seen that feasible region has no common point with  $3x + 4y < 8$

$\therefore$  Minimum value of  $Z$  is 160 at the line joining the points  $(8/3, 0)$  and  $(2, 1/2)$ .

22. Let  $l_1: 2x + 4y = 8$ ,  $l_2: 3x + y = 6$ ,  $l_3: x + y = 4$ ;  $x = 0, y = 0$

Solving  $l_1$  and  $l_2$  we get  $B\left(\frac{8}{5}, \frac{6}{5}\right)$



Shaded portion  $OABC$  is the feasible region, where coordinates of the corner points are  $O(0, 0)$ ,  $A(0, 2)$ ,

$B\left(\frac{8}{5}, \frac{6}{5}\right)$ ,  $C(2, 0)$

The value of objective function at these points are:

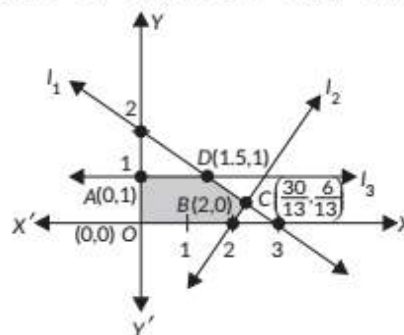
Corner points	Value of the objective function $z = 2x + 5y$
$O(0, 0)$	$2 \times 0 + 5 \times 0 = 0$
$A(0, 2)$	$2 \times 0 + 5 \times 2 = 10$ (Maximum)
$B\left(\frac{8}{5}, \frac{6}{5}\right)$	$2 \times \frac{8}{5} + 5 \times \frac{6}{5} = 9.2$
$C(2, 0)$	$2 \times 2 + 5 \times 0 = 4$

$\therefore$  The maximum value of  $z$  is 10, which is at  $A(0, 2)$ .

### Concept Applied

➤ If the region is bounded then the objective function  $Z$  has both maximum and minimum value of region.

23. Let  $l_1: 2x + 3y = 6$ ,  $l_2: 3x - 2y = 6$ ,  $l_3: y = 1$ ;  $x = 0, y = 0$



Solving  $l_1$  and  $l_3$ , we get  $D(1.5, 1)$

Solving  $l_1$  and  $l_2$ , we get  $C\left(\frac{30}{13}, \frac{6}{13}\right)$

Shaded portion OADCB is the feasible region, where coordinates of the corner points are  $O(0, 0)$ ,  $A(0, 1)$ ,  $D(1.5, 1)$ ,  $C\left(\frac{30}{13}, \frac{6}{13}\right)$ ,  $B(2, 0)$ .

The value of the objective function at these points are :

Corner points	Value of the objective function $z = 8x + 9y$
$O(0, 0)$	$8 \times 0 + 9 \times 0 = 0$
$A(0, 1)$	$8 \times 0 + 9 \times 1 = 9$
$D(1.5, 1)$	$8 \times 1.5 + 9 \times 1 = 21$
$C\left(\frac{30}{13}, \frac{6}{13}\right)$	$8 \times \frac{30}{13} + 9 \times \frac{6}{13} = 22.6$ (Maximum)
$B(2, 0)$	$8 \times 2 + 9 \times 0 = 16$

The maximum value of  $z$  is 22.6, which is at  $C\left(\frac{30}{13}, \frac{6}{13}\right)$ .

### Commonly Made Mistake

- Remember the difference between feasible solutions and infeasible solutions.

### CBSE Sample Questions

1. (b): The strict inequality represents an open half plane and it contains the origin, as  $(0, 0)$  satisfies it. (1)

2. (d): The minimum value of the objective function occurs at two adjacent corner points  $(0.6, 1.6)$  and  $(3, 0)$  and there is no point in the half plane  $4x + 6y < 12$  in common with the feasible region.

So, the minimum value occurs at every point of the line-segment joining the two points. (1)

3. (d): We have,

Corner points	Value of $Z = 3x + 9y$
$A(0, 10)$	$3 \times 0 + 9 \times 10 = 90$
$B(5, 5)$	$3 \times 5 + 9 \times 5 = 60$
$C(15, 15)$	$3 \times 15 + 9 \times 15 = 180$ (Maximum)
$D(0, 20)$	$3 \times 0 + 9 \times 20 = 180$ (Maximum)

$\therefore Z$  is maximum at  $C(15, 15)$  and  $D(0, 20)$ .

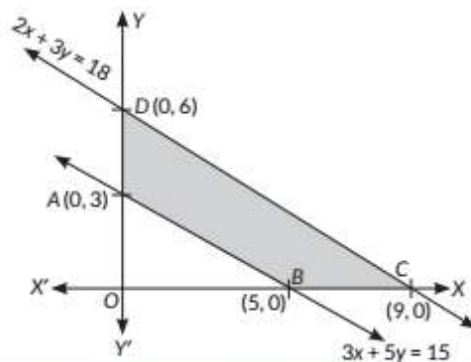
$\therefore Z$  is maximum at every point on the line joining  $CD$ . (1)

4. (c): We have,

Corner points	Value of $Z = 2x - 3y$
$(0, 0)$	$2 \times 0 - 3 \times 0 = 0$
$(0, 8)$	$2 \times 0 - 3 \times 8 = -24$ (Minimum)
$(4, 10)$	$2 \times 4 - 3 \times 10 = -22$
$(6, 8)$	$2 \times 6 - 3 \times 8 = -12$
$(6, 5)$	$2 \times 6 - 3 \times 5 = -3$
$(5, 0)$	$2 \times 5 - 3 \times 0 = 10$

$\therefore$  Value of  $Z$  is minimum at  $(0, 8)$ . (1)

5. (c): Here, the feasible region is shaded.



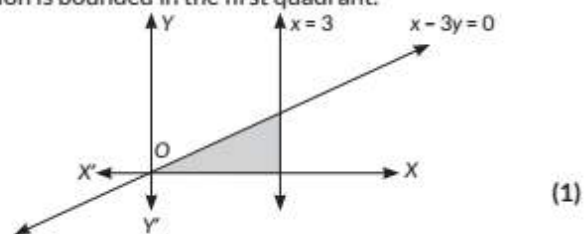
Corner points	Value of $Z = 30x + 50y$
$A(0, 3)$	$30 \times 0 + 50 \times 3 = 150$ (Minimum)
$B(5, 0)$	$30 \times 5 + 50 \times 0 = 150$ (Minimum)
$C(9, 0)$	$30 \times 9 + 50 \times 0 = 270$
$D(0, 6)$	$30 \times 0 + 50 \times 6 = 300$

Since, minimum value of  $Z$  occurs at both  $A$  and  $B$ . So,  $Z$  is minimum at every point on the line joining  $AB$ . So, minimum value of  $Z$  occurs at infinitely many points. (1)

6. (a): As,  $Z$  is maximum at  $(30, 30)$  and  $(0, 40)$ .

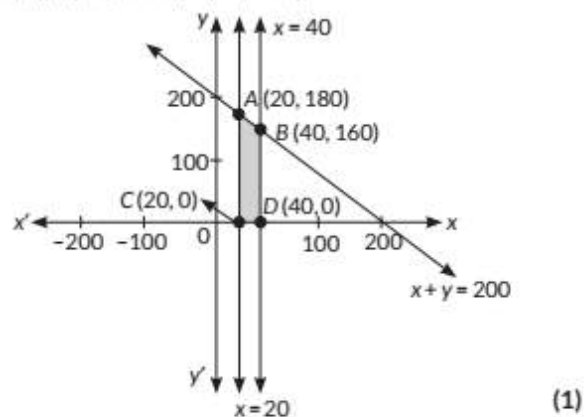
$\Rightarrow 30a + 30b = 40b \Rightarrow b - 3a = 0$  (1)

7. (b): From the graph, we can say that the feasible region is bounded in the first quadrant.



8. We have  $Z = 400x + 300y$  subject to  $x + y \leq 200$ ,  $x \leq 40$ ,  $x \geq 20$ ,  $y \geq 0$

The corner points of the feasible region are  $C(20, 0)$ ,  $D(40, 0)$ ,  $B(40, 160)$ ,  $A(20, 180)$



Corner points	$Z = 400x + 300y$
$C(20, 0)$	8000
$D(40, 0)$	16000
$B(40, 160)$	64000
$A(20, 180)$	62000

(1)

(1)

Maximum profit occurs at  $x = 40, y = 160$   
and the maximum profit = ₹ 64,000

9. Maximize  $Z = 3x + y$   
Subject to constraints

$$x + 2y \geq 100$$

$$2x - y \leq 0$$

$$2x + y \leq 200$$

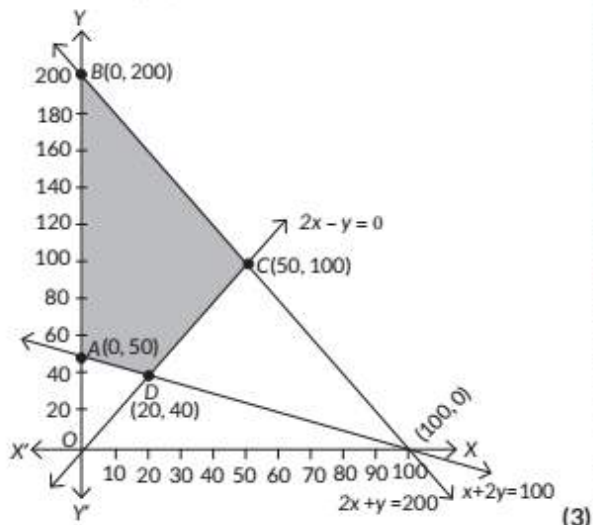
$$x \geq 0, y \geq 0$$

Converting the given inequations into equations, we get

$$x + 2y = 100 \quad \dots (i) \quad 2x - y = 0 \quad \dots (ii)$$

$$2x + y = 200 \quad \dots (iii)$$

Now, draw the graphs of (i), (ii) and (iii).



The feasible region is shaded region and corner points are  $A(0, 50), B(0, 200), C(50, 100)$  and  $D(20, 40)$ . (1)

(1) The values of  $Z$  at corner points are shown in the following table:

Corner points	$Z = 3x + y$
$A(0, 50)$	50
$B(0, 200)$	200
$C(50, 100)$	250 (Maximum)
$D(20, 40)$	100

Thus, maximum value of  $Z$  is 250 at  $x = 50, y = 100$ . (1)

10. (i)

Corner points	$Z = 3x - 4y$
$O(0, 0)$	0
$A(0, 8)$	-32 (Minimum)
$B(4, 10)$	-28
$C(6, 8)$	-14
$D(6, 5)$	-2
$E(4, 0)$	12 (Maximum)

(1½)

Thus, maximum value of  $Z$  is 12 at  $E(4, 0)$ .

and minimum value of  $Z$  is -32 at  $A(0, 8)$ . (1)

(ii) Since maximum value of  $Z$  occurs at  $B(4, 10)$  and  $C(6, 8)$ .

$$\therefore 4p + 10q = 6p + 8q \Rightarrow 2q = 2p \Rightarrow p = q \quad (2)$$

Number of optional solutions are infinite.

[ $\therefore$  Every point on the line segment  $BC$  joining the two corner points  $B$  and  $C$  also give the same maximum value] (1/2)